Euler's Method ; Spread of Infectious Disease
Math 102 Section 107

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November 20, 2017

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Answer: B. A and C are both correct, but you can simplify further!

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B. $y_2 = y_1 + (\Delta t) \cdot y_1'$

C. $y_2 = 6.1 + (0.5)(0.21)$

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Answer: It is an under-approximation, because the actual solution is *concave up*.

$$y'' = 0.1y' = 0.01(y - 4)$$

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